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Radiation-natural convection interactions in partitioned cavities

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Keywords Convection, Heat transfer, Natural convection, Partitioned cavities, Radiation

Abstract Heat transfer by radiation and natural convection in a two-dimensional, air-filled square enclosure with a vertical partition of finite thickness and varying height was investigated numerically in the laminar regime. The horizontal end walls are assumed to be adiabatic, and the vertical walls are at different temperatures. Calculations are made by using a finite volume method and an efficient numerical procedure is introduced for calculating the view factors, with shadow effects included. The results indicate that the partition does not significantly modify the heat transfer rate through the cavity, especially at high Rayleigh numbers, provided that its height is less than 90 per cent of the cavity height. The effects of radiation on the velocity and the temperature fields and the overall heat transfer rates as a function of the widths of the vents, solid/fluid conductivity ratio and Rayleigh number are documented.

v, V

= dimensional and dimensionless y velocity

Nomenclat	ure
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component = aspect ratio (A=1) А = dimensionless width of the gap, w/H W D = dimensionless thickness of the partition, d/H x,y = Cartesian coordinates Fij = view factors between surfaces Ai, Aj = dimensionless Cartesian coordinates X,Y = gravitational acceleration g H Greek symbols = enclosure height = thermal diffusivity α = thermal conductivity k = volumetric expansion coefficient ß Nucl = local convective Nusselt number Θ = dimensionless temperature, T/Th = dimensional and dimensionless pressure p.P θ = dimensionless temperature, $(T-T_0)/\Delta T$ Pr = Prandtl number, v/α σ = Stefan-Boltzmann constante = Rayleigh number, g β (Th – Tc) H³/v α Ra = Kinematic viscosity of the fluid = dimensionless distance between the parti-S = dynamic viscosity μ tion and left boundary of the enclosure, s/H εi = emissivity of the surface Ai Т = temperature = density of the fluid at To ρο = temperature of the cold wall Тс = maximal difference temperature, Th - Tc ΔT Th = temperature of the hot wall Subscripts = mean temperature, (Th + Tc) /2 То = refers to the fluid f u, U = dimensional and dimensionless x velocity = refers to the surface Ai i component р = refers to the partition

International Journal of Numerical Methods for Heat & Fluid Flow, Vol. 9 No. 1, 1999, pp. 186-203, © MCB University Press, 0961-5539 The authors wish to acknowledge gratefully the helpful assistance and discussions provided by Dr Richard Pasquetti (Laboratoire de Mathématiques, Université de Nice, France). His valuable suggestions have stimulated the authors to write the above publication.

Introduction

In recent years there have been numerous experimental and theoretical investigations of natural convection in enclosures with partition due to its considerable engineering interest, especially in building applications, for thermal insulation and passive solar heating systems. An excellent review of the past experimental and numerical studies reporting on the flow structures and heat transfer rates in enclosures with partition attached at the top wall and/or at the bottom wall, one extending upwards and the other downwards, can be found in Khan and Yao (1993).

Not so many research works were done on completely partitioned enclosures and most of them were about vertically divided cavities with very thin partition so that the heat transfer within a partition is essentially one-dimensional (Kelkar and Patankar, 1990; Nakamura and Asko, 1986). A detailed analysis on the effects of a central partition assumed either infinitely thin and isothermal at the average temperature of the hot and cold wall temperatures (ideal partition) or relatively thin was discussed by Karayiannis *et al.* (1992). It is concluded that the heat transfer rate can be calculated using the ideal partition modelling in practical engineering applications concerning air-filled enclosures. The case of multiple vertical partition was studied theoretically and experimentally by Anderson and Bejan (1981) and, numerically and experimentally by Nishimura *et al.* (1988). Both works concerned water filled enclosures and very thin metallic positions.

Probert and Ward (1974) experimentally studied the heat transfer behaviour in a partitioned enclosure of large aspect ratio. They concluded that such a configuration does not produce any significant change in the heat transfer rate across the cavity, even when the partition length equalled 90 per cent of the cavity height because this arrangement does not greatly disturb the flow. The same problem was reconsidered numerically by Kelkar and Patankar (1990) for air-filled cavity of square cross section. A study was conducted for two Rayleigh numbers (10^5 and 10^6), different widths of the gap connecting the two parts of the enclosure and perfectly conducting or adiabatic thin partition. It was shown that the reduction in heat transfer due to the partition decreases with increasing Ra because of the thinning of the horizontal boundary layers. However, plots of the mean Nusselt number versus the gap width display significant decreases in heat transfer for partition lengths greater than 90 per cent of the height of the cavity, whatever the Rayleigh number and thermal conductivity of the partition. Most recently, the effect of partition conductivity, partition heights, partition thickness and partition location on the heat transfer in a two-dimensional square enclosure is reported by Sun and Emery (1994) and Nag et al. (1994).

In all of the above mentioned studies, the influence of radiation is ignored. It can be proved for experimental works in which water or other liquid is used as the working fluid while it is rather surprising that the assumption of neglecting the effect of radiation is not even mentioned in many of the theoretical studies which dealt with complex gas-filled enclosures. For example, the effect of radiation exchanges between surfaces on natural convection is known to be important, Radiationnatural convection

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even at room temperature, in air-filled cavities the walls of which are not maintained at prescribed temperatures or perfectly reflecting. For partitioned cavities, the radiation-convection interaction to the partition should be considered in a number of practical situations for which the emissivities of the surfaces are generally high. As far as the authors are aware, the paper of Chang et al. (1983) is the only one in which interaction of radiation and natural convection was considered for an enclosure partitioned by two vertical adiabatic partitions of finite-thickness and equal length located at the ceiling and floor. Both surface and gas radiation effects were studied and it is shown that the predominant mechanism by which radiation process increases the overall heat transfer rates is the surface radiation. For the asymptotic case of a completely partitioned cavity, the heat transfer rate by radiation modifies the surface temperatures of the partition, and therefore, the natural convection flow is strongly affected by radiation. A very thin vertical partition located within a rectangular differentially heated cavity acts as a radiation screen. In this case, it is known that approximate analyses based on analogous electrical circuits provide quite accurate estimates of the effect of a partition assumed to be very thin and located at the mid-section of a rectangular cavity was carried out by Nakamura and Asko (1986). It was shown that the emissivities of the top and bottom walls only slightly affect the heat transfer by convection in both cases of conductive and insulated top and bottom walls. On the other hand, the emissivities of the cold and hot walls and of the partition were shown to modify considerably the convection heat transfer.

This paper describes the effect of adding a thick partition located vertically close to the hot wall of a differentially heated cavity, forming a narrow vertical channel in which the flow is controlled by vents at the bottom and top of the partition as shown in Figure 1. A numerical examination of radiationconvection interaction is presented, the focus being on engineering applications at room temperatures and for enclosures filled with air (non-participating gas). It is shown that radiation has a significant influence on the flow and heat transfer in the channel. In this study, the sizes of the vents and thermal conductivity of the partition are other parameters of interest.



Figure 1. The geometry considered

Mathematical model

Details of the geometry are shown in Figure 1. The flow is assumed to be incompressible, laminar, stead and two-dimensional in an enclosure of square cross-section, the horizontal end walls are perfectly insulated while the two vertical walls are maintained at two different temperatures T_h and T_c respectively. To simplify the analyses, the Boussinesq approximation is invoked. The working fluid is air and its physical properties except density are assumed to be constant at the average temperature of T_h and T_c . Radiation exchanges in the enclosure are considered to be between opaque, diffuse and grey surfaces.

The equations are nondimensionalized using the following definitions of the dimensionless variables (see the nomenclature):

X = x/H	•	Y = y/H
$U = uH/\alpha$;	$V = vH/\alpha$
$\theta = (T - T_o)/(T_h - T_c)$;	$P = (p + \rho_0 gy)H^2/\rho_0 \alpha^2$

the dimensionless governing equations in the fluid domain can be expressed as: Continuity:

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0 \tag{1}$$

X momentum:

$$U\frac{\partial U}{\partial X} + V\frac{\partial U}{\partial Y} = -\frac{\partial P}{\partial X} + \lambda \Pr\left[\frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2}\right]$$
(2)

Y momentum:

$$U\frac{\partial V}{\partial X} + V\frac{\partial V}{\partial Y} = -\frac{\partial P}{\partial Y} + \lambda \Pr\left[\frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2}\right] + Ra \Pr \theta$$
(3)

Energy:

$$U\frac{\partial\theta}{\partial X} + V\frac{\partial\theta}{\partial Y} = R_k \left[\frac{\partial^2\theta}{\partial X^2} + \frac{\partial^2\theta}{\partial Y^2} \right]$$
(4)

Where λ and R_k are equal to 1 in the fluid region and $\lambda = \infty$, $R_k = k_p/k_f$ in the solid region.

The thermal condition at the surface of the partition is determined by a balance between radiation, conduction and convection as:

$$R_k \frac{\partial \Theta_p}{\partial n} = \frac{\partial \Theta}{\partial n} - N_r Q_r \tag{5}$$

Where $N_r = \sigma T_h^4 / (k_f \frac{\Delta T}{H})$ the radiation number, Q_r the dimensionless net radiation flux and " \vec{n} " denotes the unit normal vector to the surface at the partition-air interface.

For the insulated bottom and top walls, the following balance applies:

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$$0 = \frac{\partial \theta}{\partial Y} - N_{\Gamma} Q_{\Gamma} \tag{6}$$

The cold and hot walls are maintained at dimensionless temperatures of -0.5 and 0.5 respectively. For the velocity field, the boundary conditions are of the noslip type.

The equations (5) and (6) are discretized. In order to do this the radiating surface of the solid forming the enclosure and the partition is divided into a number of surfaces A_i , i = 1, ..., N. Therefore, the dimensionless net radiative flux density along a diffuse grey surface " A_i " is expressed as:

$$Q_{r,i} = R_i - H_i \tag{7}$$

Where R_i and H_i are the dimensionless radiosity and incident radiation:

$$R_{i} = \varepsilon_{i} \Theta_{i}^{4} + (1 - \varepsilon_{i})H_{i}$$

$$\tag{8}$$

Where the dimensionless radiative temperature Θ_i is given by:

$$\Theta_i = T / T_h = \left[(T_h - T_c) \ \theta_i + T_o \right] / T_h \tag{9}$$

For an enclosure consisting of N nonisothermal surfaces such that the radiative properties are uniform over each surface, the radiation flux arriving at surface A_i may be expressed as:

$$H_{i} = \sum_{j=1}^{N} R_{j} F_{i-j}$$
(10)

The diffuse view factors between the two isothermal surfaces, F_{i-j} , depends only on their positions and orientations. For further details on the expression of the net radiative flux, the reader can refer to Siegel and Howell (1972).

The heat flux at the side isothermal walls is the sum of the conductive and radiative fluxes. In dimensionless form, the local heat flux is defined as follows:

$$\frac{q_{W}}{(k_{f}\Delta T/H)} = -\frac{\partial \theta}{\partial X} |_{X_{W},Y} + N_{r} Q_{r}(X_{W},Y)$$
(11)

Where $X_w = \{0, 1\}$. Therefore, an overall local Nusselt number may be introduced such as:

$$Num(X_{W}, Y) = Nu_{c}(X_{W}, Y) + Nu_{r}(X_{W}, Y)$$
(12)

Where Nu_c and Nu_r are the convective and radiative contributions in Num. The average Nusselt numbers along the side walls are determined as:

$$Num(X_w) = \int_0^A \left(-\frac{\partial \theta}{\partial X} \mid X_w, Y + N_r Q_r(X_w, Y) \right) dY$$
(13)

For adiabatic end walls, Num(0) = Num(1).

Finally, the volumetric exchange flow rates through the bottom and top vents which are defined as:

$$\psi_{thru} = \int_0^W |U| \, dY = \int_{A-W}^A |U| \, dY \tag{14}$$

The solution of these equations is dependent on a large set of parameters. These are Pr, Ra, R_k, A, D, W, and S for the conjugate problem without radiation. When including the effect of radiative exchange between surfaces, the above set must be completed by three parameters: Nr, T_0 , ε_i . In this paper, the aspect ratio and Prandtl number are set constant (A = 1, Pr = 0.71) and the reference temperature is set to be at $T_0 = 290$ K. Furthermore, the geometry and location of the partition wall are defined by D = 0.05 and S = 0.1. Thus, the only geometrical parameter which will be varied in the following is the width of the vents ($0 \le W \le 0.20$).

Numerical procedure

The governing differential equations were solved by a finite-volume method which utilizes a send-order central difference scheme for the advective terms in order to reduce numerical diffusion errors. In the range of Ra numbers investigated, the CDS solution did not exhibit spurious oscillations and the convergence was achieved by using small underrelaxation factors on U, V and θ . The SIMPLER algorithm for pressure-velocity coupling was adopted (Patankar, 1980). The governing equations were cast in transient form and a fully implicit transient differing scheme was employed as an iterative procedure to reach steady-state. The presence of the partition was accounting by the strategy in which it was characterized by a region of very high viscosity.

The resulting systems of discretized equations were solved by an iterative procedure based on a preconditioned conjugate gradient method. The outer iterative loop was repeated until the following convergence are simultaneously satisfied:

$$\max |\phi^{n+1} - \phi^n| < \varepsilon_{\phi} \tag{15}$$

Where ϕ is a dependant variable and n the iteration number (i.e. false time step). In most of the cases, the velocity components and temperature were driven to $\varepsilon_u = \varepsilon_v = \varepsilon_\theta < 10^{-6}$. For the pressure correction equation, which is a discretized Poisson equation, the iterative process was stopped when the maximum residual of mass (amount by which the continuity equation was not satisfied) was less than 10^{-8} .

For the combined radiation and convection problem, the surface temperatures on the partition and on the adiabatic end walls were calculated from the non-linear heat balance equation (equations (5) and (6)) by using an inner iterative procedure at every time step for the energy equations. The grid was extended across the adiabatic boundaries by introducing one extra point in order to discretise equations (5) and (6). The surface temperatures were updated from the solution of the energy equation by under-relaxing the boundary 191

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evaluation of temperature. At each inner iteration, the linear system of equations for the radiosities was solved by a direct method (Gauss elimination). The grid was constructed such that the boundaries of the physical domain coincide with the velocity grid lines. The points for pressure and temperature were placed at the center of the scalar volumes. At the fluid-partition interfaces, the control volume faces were also arranged so that a control volume face coincide with an interface. This grid distribution was chosen to ensure the interface energy balance. To avoid a checkboard pressure and velocity fields, staggered grids were used for the U and V-velocity components in the Y and Xdirections respectively.

Computation of radiation

Since the radiative properties of the solid surfaces of the enclosure vary from point (even on the isothermal side walls because the incident radiation cannot be assumed as uniform), each of the surface was divided into finite number of zones on which the four basic assumptions of the simplified zone analysis was assumed valid. The number of zones retained was determined by the mesh used to solve the differential equations. Therefore, the zoning was nonuniform and the area of each zone varied according to the stretching function and number of grid points used. For N control volume faces, this results in N(N-1)/2 view factors to be calculated and in a linear system of N equations for the radiosities. In view of the meshes used, N was typically of the order of 250. The view factors were determined by using a boundary element approximation (Mezrhab, 1991). This method is summarized here for a two-dimensional geometry including shadow effects. Consider two surfaces A_i and A_i, as shown in Figure 2, very long in the direction perpendicular to the plane of the figure. Let l_i and l_i be the lengths of the arcs corresponding to surfaces A_i, A_i in the plane of the figure. For this 2D-geometry, the view factor between A_i and A_j reduces to:

$$F_{i-j} = \int_{I_i} \int_{I_j} \frac{\cos \theta_i \cos \theta_j}{2 r_{ij}} \alpha_{ij} dI_i dI_j$$
(16)

Where θ_i (θ_j) is the angle of the outward normal to dl_i (dl_j) with the r_{ij} joining these two elemental surfaces, and α_{ij} a function such as $\alpha_{ij} = 0$ when shadow effects occur or if $\theta_i(\theta_i) \ge \pi/2$ and $\alpha_{ij} = l$ otherwise.



Figure 2. Radiative exchange between surfaces A_i and A_j The approximation of a length l by boundary elements consists in the discretization of l into elementary surfaces l_i and approximating each one by a polynomial vector function $F(\eta)$ where η is curvilinear coordinates associated with the element (see e.g. Brebbia *et al.*, 1984; Caruso, 1988).

The element is characterized by the degree of a single variable interpolation polynomial and thus the number of interpolation points associated with it, as illustrated in Figure 3. The polynomial approximation of the position vector, $r(\eta)$, reads:

$$r(\eta) = \sum_{\rho=1}^{P} \varphi_{\rho}(\eta) r_{\rho},$$
(17)

Where $\overrightarrow{r_p}$ is the positive vector of the point M_p and where $\phi_p(\eta)$ is the Lagrange's polynomial of degree (P–1) such that:

$$\varphi_{\rho}(\mathcal{M}_{q}) = \varphi_{\rho}(\eta_{q}) = \delta_{\rho q} \tag{18}$$

with δ_{pq} the Kronecker symbol.

The calculation of a curvilinear integral requires the transformation factor:

$$J = \left| \frac{\overrightarrow{\partial r}}{\partial \eta} \right| = \left| \sum_{\rho=1}^{P} \frac{\partial \varphi_{\rho}(\eta)}{\partial \eta} \stackrel{\rightarrow}{r}_{\rho} \right|$$
(19)

Using this procedure for the evaluation of the view factor between two boundary elements of length l_i and l_j leads to:

$$\cos\theta_i dl_i = \frac{\overrightarrow{r}_{ij} \overrightarrow{n_i}}{r_{ij}} dl_i = J_i d\eta_i \cdot \frac{\overrightarrow{r}_{ij} \overrightarrow{n_i}}{r_{ij}}$$
(20)

Let $\overrightarrow{G}_i = J_i \overrightarrow{n_i}$.

By writing a similar expression for $\cos \theta_i dl_i$, we obtain, with $-1 \le \eta \le 1$:

$$F_{i-j} = -\frac{1}{l_i} \int_{-1}^{1} \int_{-1}^{1} \frac{(\vec{G}_i \cdot \vec{r}_{ij}) (\vec{G}_j \cdot \vec{r}_{ij})}{2 r_{ij}^9} \alpha_{ij} d\eta_i d\eta_j$$
(21)



Figure 3. Curve fitting by boundary elements

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Real Element

Boundary Element

Where

$$I_{j} = \int_{-1}^{1} \left| \frac{\partial \overrightarrow{r_{j}}}{\partial \eta_{j}} \right| d\eta_{j}$$
(22)

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In the present study, we used rectilinear boundary elements and Lagrange polynomials with $\eta_p = 0$ if M_p is at the element center. Therefore, the liner approximation of $\overrightarrow{r_p}$ is based on the following polynomials:

$$\varphi_1(\eta) = (1 - \eta)/2$$
; $\varphi_2(\eta) = (1 + \eta)/2$ (23)

The calculation of the integral is performed by using a Monte Carlo method because this method is well suited for multidimensional integration. The algorithm is based on a discretization of the integration domain (square of unit side in two dimensions) into a set of sub-volumes.

In the present study, the partition acts as a screen. The aim is now to produce an efficient algorithm for the calculation of α_{ij} . This algorithm can be explained through Figure 4: the element l_k intercepts the radiation going from *a* on l_i to *b* on l_j (see Figure 2) if the quadrilateral abcd is convex. This can be checked by introducing four vectors \vec{N}_{ab} , \vec{N}_{bc} , \vec{N}_{cd} , and \vec{N}_{da} normal to the four sides *ab*, *bc*, *cd* and *da*. If the element l_k intercepts the radiation from *a* to *b*, then:

$$(N_{ab}.ac) (N_{ab}ad) > 0$$

$$\rightarrow \rightarrow \rightarrow \rightarrow$$

$$(N_{bc}.ba) (N_{bc}bd) > 0$$

$$\rightarrow \rightarrow \rightarrow \rightarrow$$

$$(N_{cd}.ca) (N_{cd}cb) > 0$$

$$\rightarrow \rightarrow \rightarrow \rightarrow$$

$$(N_{da}.db) (N_{da}dc) > 0$$

$$(24)$$

If three of these requirement are satisfied, then the fourth is satisfied also. When using the Monte Carlo method for calculating the view factors, the points *a* and



Figure 4. Radiative exchange between surfaces with screening effects *b* were randomly generated into each of the sub-volumes, until the convergence of the calculation is reached, i.e. until the relative desired accuracy is obtained.

For the present combined convection and radiation problem, the boundary elements were straightforwardly chosen as the N faces of the control volumes lying on the solid surfaces. For each of the boundary elements, the summation rule was checked and it has found that all the view factor summations verified the conditions $\sum_{j=1}^{N} F_{i\cdot j} = 1 \pm 0.0001$.

Code validation

The code was extensively exercised on benchmark problems to check its validity. Calculations were first performed for the classical problems of flow in a square driven cavity and for natural convection in differentially heated cavities of various aspect ratios. Next, natural convection in partitioned enclosures was considered. In this section, a comparison of our results with those recently reported by Janssen and Henkes (1993) for natural convection in a square cavity is present for $Ra = 10^6$ and 10^8 . Then, the solutions obtained for a square partitioned enclosure are compared with those of Kelkar and Patankar (1990).

Table I allows a comparison of the present results for three quantities selected in (Janssen and Henkes, 1993): the averaged wall heat transfer Nu along the hot vertical wall, the maximum V_{max} of the vertical along the horizontal velocity along the vertical line through the cavity center. It should be noted that the velocity scales used in (Janssen and Henkes, 1993) are $(g\beta\Delta Tv)^{1/3}$ for U and $(g\beta\Delta TH)^{1/2}$ for V. Therefore, the present U and V-velocity components reported in Table I were multiplied by $(RaPr^2)^{1/3}$ and $(RaPr)^{1/2}$ respectively. As can be seen, all the quantities are in very good agreement with those of Janssen and Henkes (1993). In addition, the deviation with respect to the reference solution of Le Quéré (1991) are very small for the finest grid. We have used the same grid

Grid	Ra	Num. Ra ^{-1/4}	V _{max}	U _{max}	
Janssen and Henke	s				_
30×30	106	0.2782	0.2658	0.8174	
	108	0.2977	0.2794	0.8069	
60 imes 60	10^{6}	0.2789	0.2633	0.8145	
	10^{6}	0.2789	0.2633	0.8145	
	108	0.3013	0.2647	0.8528	
120×120	10^{6}	0.2790	0.2621	0.8144	
	108	0.3020	0.2643	0.8769	
Present					
30×30	10^{6}	0.2800	0.2619	0.8179	
	108	0.3067	0.2601	0.7916	
60 imes 60	10^{6}	0.2792	0.2632	0.8154	Table I.
	108	0.3034	0.2651	0.8520	Comparison of test case
120×120	10^{6}	0.2791	0.2626	0.8125	with solutions of
	108	0.3025	0.2644	0.8643	Janssen and Henkes

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which in the horizontal direction, the stretching function chosen for the U velocities is:

$$X = \frac{i}{i_{\text{max}}} - \frac{1}{2\pi} \sin(2\pi \frac{i}{i_{\text{max}}}), \ i = 0, ..., i_{\text{max}}$$

Where i_{max} refers to the number of grid points in X direction.

In the work of Kelkar and Patankar (1990), the centrosymmetry property of the solution was introduced and the governing equations were solved in half of the physical domain. In the present study, the boundary conditions do not possess symmetry properties owing to the radiative heat transfer terms. Therefore, all the computations were carried out on the whole domain, even for the test case discussed in this section. Figure 5 shows the variation of the average Nusselt number and flow rates (equation (14)) with gap width for two Rayleigh numbers and for perfectly conducting partitions as well as for perfectly insulated partitions located in the vertical middle plans of a square, differentially heated cavity. Like in Kelkar and Patankar (1990), we considered very thin partitions. As can be seen in Figure 5, both heat transfer and flow rates decrease with a decreasing gap width. These results can be favourably compared with those displayed in Figure 2 of Kelkar and Patankar (1990). Despite any numerical data were reported in Kelkar and Patankar (1990), the largest discrepancies between the present results and those graphically shown in Kelkar and Patankar (1990) can be estimated to be less than 3 per cent.

When we include the radiation, the code was validated with results obtained in Kassemi and Naraghi (1993) for all the cases with the transparent fluid in enclosure. At the same problem, we obtain the same flow and temperature profiles, and the differences between our and published results for the Nusselt number are less than 2 per cent.

Based on the above studies, it was concluded that the code could be reliably applied to the problem under consideration.



Figure 5.

Variation of: (a) overall Nusselt number; and (b) throughflow strength with gap width for different Rayleigh numbers

Results and discussion

A preliminary study was carried out to determine the optimum nonuniform grid (i.e. the best compromise between accuracy and computational costs). For the calculations reported in this study a 41×41 grid points was chosen to optimise the relation between the accuracy required and the computing time. The grid is nonuniform and is fine near the solid surfaces and tips of the partition. Increasing the number of grid points did not change the results appreciably. For example, adding 20 grid lines in each direction changed the Nusselt number by less than 1 per cent for all values of Ra.

Each case required the specification of seven dimensionless parameters (Ra, Pr, R_k, A, S, D, W) among which the Prandtl number, the cavity aspect ratio, the gap width between the partition and the hot wall and the partition thickness were held fixed at Pr = 0.7, A = 1, S = 0.1 and D = 0.05 respectively. The ranges covered by the remaining parameters were $10^3 \le \text{Ra} \le 10^8$, $0 \le W \le 0.2$ and $0 \le R_k \le \infty$. The three dimensional parameters corresponding to computations of radiation are fixed as: Nr = 30, $\varepsilon_i = 1$ for $1 \le i \le N$ and $\Delta T/T_0 = 0.12$.

radiation are fixed as: Nr = 30, $\varepsilon_i = 1$ for $1 \le i \le N$ and $\Delta T/T_0 = 0.12$. For $R_k = 30$, W = 0.025 and $Ra = 10^6$, Figures 6 and 7 show the isotherms and streamlines respectively for Nr = 0 (i.e. in the absence of radiation) and for Nr =30 (i.e. the presence of radiation). From the temperature contours, it appears that the radiation heat transfer produces a good homogenization of temperature especially in the cold part of the enclosure: the temperature stratification is less pronounced and the core of the fluid becomes warmer when compared to the natural convection case. It is seen in Figure 8 that the radiation reduces the difference between the top and bottom temperatures. The temperature gradients near the horizontal walls give an indication of the importance of radiative flux. Along a cold wall, the gradients of termperature are less important on the high part of cavity for Nr = 30, than in the low part of cavity. The average convective Nusselt number is also less when we take into account the radiation. One can see also, that the streamlines shown in the case with Nr = 0 are very similar to those including radiation. When Nr = 30, the streamlines indicate that the central vortices become weaker. Note, however, that the flow near the cold wall remains strong in order to dissipate the extra heat delivered







Radiationnatural convection by radiation into the cold sink. It is observed that the radiation effects increase the vertical velocity near the cold wall by 5 per cent. This is owing to the increase of the flow rate through the bottom and the top vents. As a matter of fact, the difference between the average fluid temperatures in the left part and the right part of cavity increase with radiation, the circulation increases in the channel delimited by the hot wall and the partition.

Nusselt number

The effect of the width of the vents on heat transfer rate was first examined for R_k = 30 (i.e. k_p \cong 1 W/m.K) for various Ra. Figure 9 shows that the presence of the partition has a significant influence on Num provided W < 0.1. The effect of \hat{W} on the Nusselt number is weaker until $Ra = 10^4$ because the circulation of air is weak, thus the conduction is the principal mode of heat transfer. It is observed an increasing of Num with W for $W \le 0.1$ and $Ra \le 10^6$, it is the same for $W \le 0.05$ and $Ra \ge 10^7$. The radiation increases the overall average Nusselt number for all values of W and Ra, however, this increasing is less pronounced as Ra is high. For example, for Nr = 30, the effect of radiation is to multiply Num by 6 if Ra = 0, and by 2 if Ra = 10^5 whereas the increasing is only in the order



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Figure 8. Wall temperature

W=0.025

Figure 7.

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of 7 per cent for $Ra = 10^8$. For all simulations which correspond to Figure 9, the radiative Nusselt number Nu_r on the hot wall is comprised between 3 and 4.5. Consequently, the radiative contribution in combined heat transfer becomes weaker and weaker as Ra increase.

The variation of the convective portion in local Nusselt number on the hot wall, Nucl = Nu_c (0,Y), is shown in Figure 10. It can be seen that the radiation increases Nucl in the bottom portion near the hot wall for Ra = 10^5 and decreases Nucl for Ra = 10^8 . This is explained one more time by the throughflow strength which is very important at moderate Ra. At high Ra, the circulation induced by the buoyancy force is important and the principal effect of radiation is also to reduce the convective heat transfer on the hot wall (the same throughflow like two hot surfaces instead of one surface).

Throughflow strength

Figure 11 shows the variation of Ψ_{thru} with W for $10^5 \le \text{Ra} \le 10^8$. For $\text{Ra} \le 10^4$, Ψ_{thru} is smaller even if it increases under the radiation effect, and its maximal value is about 0.3 when the width of the vents is inferior at 0.2. At $\text{Ra} = 10^5$, the







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radiation effect on the Ψ_{thru} is significant from W \leq 0.15, we can also note an increasing in the order of 8 per cent. For W = 0.025, the increasing of Ψ_{thru} under the effect radiation begin from Ra \geq 10⁷.

Effect of partition conductivity

The computations were carried out for two dimensionless conductivity ratio ($R_k = 0 \text{ and } \infty$) and for a fixed width of the vents (W = 0.025). The results obtained for $R_k = \infty$ are similar to those obtained for $R_k = 30$. The effect of partition conductivity on the Nusselt number is shown in Figure 12 for Nr = 0 and Nr = 30.

When $R_k = 0$, the value of the Nusselt number is weak for $Ra \le 10^5$ because the fluid gets hot due to its inability to transfer heat through the adiabatic wall. Otherwise, the heat transfer from the hot wall to the cold wall is made by the vents and, since W is small, the flow is only generated if $Ra \ge 10^5$. (For W = 0, we have obviously Num = 0 for all values of Ra). When $Ra \ge 10^5$, the transferred heat flux increase rapidly and for $Ra = 10^8$, the partition do not decrease practically the heat transfer. If we take into account the radiation, we observe that the transferred radiative flux is small due to the obstacle played by the partition. The order of its contribution in the Nusselt number is 50 per cent on





Figure 12. Effect of partition conductivity on the Nusselt number

the hot wall for $Ra = 10^5$. It decreases when Ra increases and is only 10 per cent at $Ra = 10^8$. The variation of the local convective Nusselt number along the hot wall (Figure 13) confirms the strong obstacle effect played by the partition at Ra = 10^5 and its weak influence at $Ra = 10^8$. It is shown too that the convective contribution in the overall average Nusselt number is, in this case, slightly modified by the radiation.

When $R_k = \infty$, the isolating effect of the partition is less important. However, the rubble effect on the circulation of the fluid is reinforced. We have also Num \geq 1 for all values of Ra. It can be explained easily: if the Rayleigh number is very small, in order that the fluid circulates between the hot wall and the partition, the heat is transferred by conduction in the fluid lane and the partition. The problem is also similar to the one of the cavity differentially heated with a thermal resistance on the hot wall. When Ra increases, we observe that the overall average Nusselt number becomes almost independent of the partition conductivity from $Ra \cong 2.10^6$. It is, however, slightly inferior to the one obtained for $R_k = 0$. Because the circulation of the fluid is made essentially in the cold part of the cavity, the aspiration effect is also weaker than for $R_k = 0$. Finally, though the nature of flow is sensibly affected by the value of the partition conductivity, the heat flux transferred at high Rayleigh number ($Ra \approx 10^8$) is almost independent of the partition conductivity, of the exchange by radiation and of the width of the vents when the one is superior at 2.5 per cent of the height of the cavity. The calculations of the throughflow through the vents and the velocity profile confirms this commentary made in Figure 12.

Conclusions

A numerical study of natural convection and radiation in partitioned square enclosure, differentially heated, has been presented. Within the investigated parameter ranges, the following conclusions can be drawn.

(1) For all values for Ra, the effect of the partition may be negligible if the width of the vents is superior at W = 0.1.





- (2) For a given value of W, the effect of the partition becomes negligible when Ra is high.
- (3) The radiation standardizes the temperatures in the two parts of the cavity and increases the difference between the average temperatures, increases the rate of the fluid in the space delimited by the wall and the partition (channel effect). Its effect is to increase the circulation in all the enclosure.
- (4) Our study was carried with parameter radiation Nr = 30, which corresponds to moderate difference temperature between the hot and cold wall. However, we have observed that the radiation plays a very important role in the overall heat transfer and the one is enhanced significantly if the radiation is included.

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